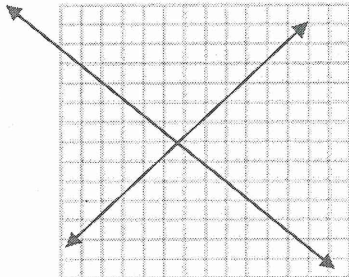


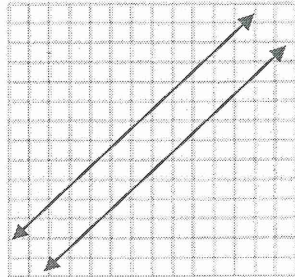
1. Describe everything you know about each system that is graphed:

a.



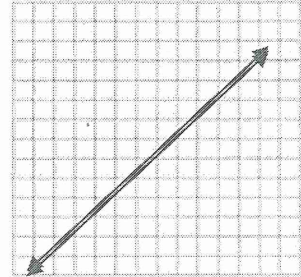
One solution

b.



- No Solution  
 - Lines are  $\parallel$   
 - Lines have the same slope

c.



- Infinitely many solutions  
 - Two equations describing the same line

2. Is (6, 9) a solution to the system  $\begin{cases} y = 3x + 1 \\ y = 2x - 5 \end{cases}$ ?

Why or why not?

$$\begin{cases} y = 3(6) + 1 = 18 + 1 = 19 & (6, 19) \\ y = 2(6) - 5 = 12 - 5 = 7 & (6, 7) \end{cases}$$

Neither line goes through the point (6, 9); therefore, it cannot be a solution to the system of equations.

3. Describe what you know about the system  $\begin{cases} 3x + 2y = 6 \\ y = x - 7 \end{cases}$

if (4, -3) is the solution.

If (4, -3) is the solution, then an input value of 4 in both  $3x + 2y = 6$  and  $y = x - 7$  should give me an output value of -3. (The point (4, -3) is on both lines.)

4. The sum of two numbers is 16 and their difference is 8. What are the two numbers? Show how a system of equations can be used to find the numbers.

$$\begin{array}{r} \begin{cases} x + y = 16 \\ x - y = 8 \end{cases} \\ + \\ \hline 2x = 24 \\ \frac{2x}{2} = \frac{24}{2} \\ *x = 12 \end{array}$$

$$\begin{array}{r} (12) + y = 16 \\ -12 \quad -12 \\ \hline *y = 4 \end{array}$$

$(12, 4)$

5. Solve each system by elimination:

$$\begin{cases} x + y = -3 \\ 2x - 3y = -11 \end{cases} \cdot 2$$

$$\begin{array}{r} 2x + 2y = -6 \\ -2x - 3y = -11 \\ \hline 0x + 5y = 5 \\ y = 1 \end{array}$$

$$\begin{array}{r} x + (1) = -3 \\ -1 \quad -1 \\ \hline x = -4 \end{array}$$

$(-4, 1)$

$$\begin{cases} 4x + 5y = 3 \\ 2x + 5y = -11 \end{cases}$$

$$\begin{array}{r} 4x + 5y = 3 \\ -2x + 5y = -11 \\ \hline 2x + 0y = 14 \\ \frac{2x}{2} = \frac{14}{2} \\ x = 7 \end{array}$$

$$\begin{array}{r} 2(7) + 5y = -11 \\ 14 + 5y = -11 \\ -14 \quad -14 \\ \hline 5y = -25 \\ \frac{5y}{5} = \frac{-25}{5} \\ y = -5 \end{array}$$

$(7, -5)$

$$\begin{cases} x - 3y = 2 \\ -x + 2y = -3 \end{cases}$$

$$\begin{array}{r} x - 3y = 2 \\ -x + 2y = -3 \\ \hline -y = -1 \\ y = 1 \end{array}$$

$$\begin{array}{r} x - 3(1) = 2 \\ x - 3 = 2 \\ x = 5 \end{array}$$

$(5, 1)$

$$\begin{cases} 4x - y = 5 \\ 3x + y = 9 \end{cases}$$

$$\begin{array}{r} 4x - y = 5 \\ 3x + y = 9 \\ \hline 7x = 14 \\ \frac{7x}{7} = \frac{14}{7} \\ x = 2 \end{array}$$

$$\begin{array}{r} 3(2) + y = 9 \\ 6 + y = 9 \\ y = 3 \end{array}$$

$(2, 3)$

$$\begin{cases} 2x - 5y = -7 \\ -2x + 3y = 1 \end{cases}$$

$$\begin{array}{r} 2x - 5y = -7 \\ -2x + 3y = 1 \\ \hline -2y = -6 \\ \frac{-2y}{-2} = \frac{-6}{-2} \\ y = 3 \end{array}$$

$$\begin{array}{r} 2x - 5(3) = -7 \\ 2x - 15 = -7 \\ 2x = 8 \\ x = 4 \end{array}$$

$(4, 3)$

6. Solve each system by substitution:

$$\begin{cases} x + 3y = 12 \\ x - y = 4 \end{cases}$$

$$\begin{array}{r} x + 3y = 12 \\ x - y = 4 \\ \hline x = y + 4 \end{array}$$

$$\begin{array}{r} (y + 4) + 3y = 12 \\ 4y + 4 = 12 \\ -4 \quad -4 \\ \hline 4y = 8 \\ y = 2 \end{array}$$

$$\begin{array}{r} x = y + 4 \\ x = 6 \end{array}$$

$(6, 2)$

$$\begin{cases} x + 4y = 1 \\ 2x + 7y = 6 \end{cases}$$

$$\begin{array}{r} x + 4y = 1 \\ 2x + 7y = 6 \\ \hline x = -4y + 1 \end{array}$$

$$\begin{array}{r} 2(-4y + 1) + 7y = 6 \\ -8y + 2 + 7y = 6 \\ -y + 2 = 6 \\ -y = 4 \\ y = -4 \end{array}$$

$$\begin{array}{r} x + 4(-4) = 1 \\ x - 16 = 1 \\ x = 17 \end{array}$$

$(17, -4)$

$$\begin{cases} -x + y = 9 \\ x + 2y = 6 \end{cases}$$

$$\begin{cases} 2x - 3y = 9 \\ 5x + 3y = 12 \end{cases}$$

$$\begin{cases} -4x - y = 11 \\ 4x + 4y = -20 \end{cases}$$

7. The Free State Frisbee club sold Free State Frisbees to raise money. Green discs with the words Free State engraved on them sold for \$4 each, and custom made discs with the Firebird emblem engraved on them sold for \$20 each. On the first day of sales, the club had sold 38 Frisbees and earned \$200. How many Frisbees of each type were sold on the first day?

x: Green \$4/ea  
y: Custom \$20/ea

$$\begin{cases} x + y = 38 \\ 4x + 20y = 200 \end{cases}$$

$$y = 38 - x$$

$$\begin{array}{r} 4x + 20(38 - x) = 200 \\ 4x + 760 - 20x = 200 \\ -16x = -560 \\ x = 35 \end{array}$$

$$\begin{array}{r} 35 + y = 38 \\ y = 3 \end{array}$$

$(35, 3)$