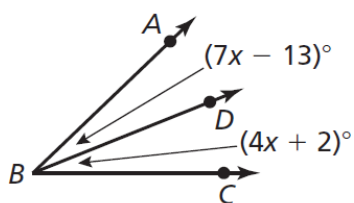
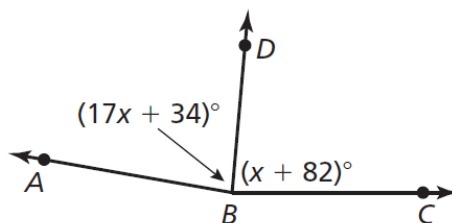


\overline{BD} bisects $\angle ABC$. Find $m\angle ABD$ and $m\angle CBD$.

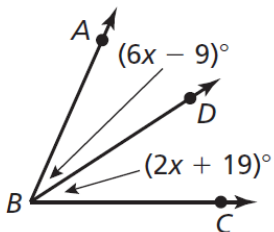
1.



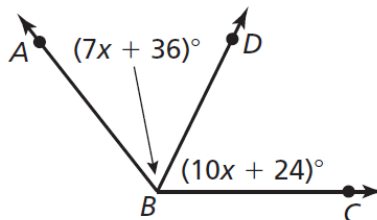
2.



3.



4.



Essential Question

In a diagram, what can be assumed and what needs to be labeled?

\overleftrightarrow{AF} and \overleftrightarrow{BD} are perpendicular.

\overleftrightarrow{EG} and \overleftrightarrow{BD} are parallel.

\overleftrightarrow{AF} and \overleftrightarrow{BD} are coplanar.

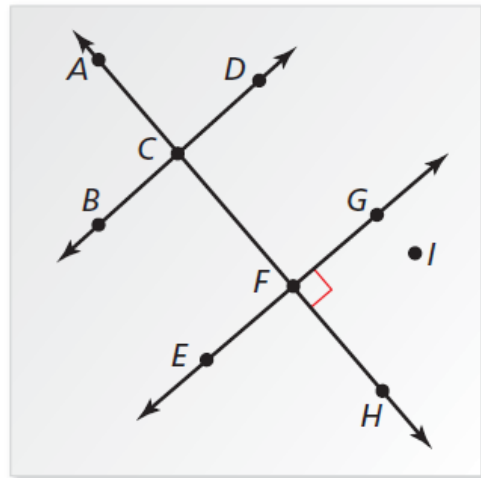
\overleftrightarrow{EG} and \overleftrightarrow{BD} do not intersect.

\overleftrightarrow{AF} and \overleftrightarrow{BD} intersect.

\overleftrightarrow{EG} and \overleftrightarrow{BD} are perpendicular.

$\angle ACD$ and $\angle BCF$ are vertical angles.

\overleftrightarrow{AC} and \overleftrightarrow{FH} are the same line.



Postulates

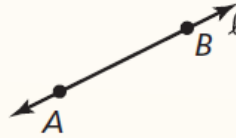
Point, Line, and Plane Postulates

Postulate

Example

2.1 Two Point Postulate

Through any two points, there exists exactly one line.



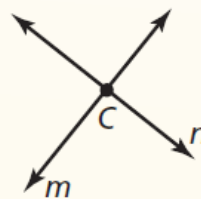
Through points A and B , there is exactly one line ℓ . Line ℓ contains at least two points.

2.2 Line-Point Postulate

A line contains at least two points.

2.3 Line Intersection Postulate

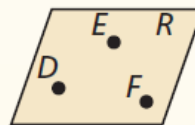
If two lines intersect, then their intersection is exactly one point.



The intersection of line m and line n is point C .

2.4 Three Point Postulate

Through any three noncollinear points, there exists exactly one plane.



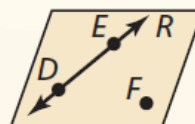
Through points D , E , and F , there is exactly one plane, plane R . Plane R contains at least three noncollinear points.

2.5 Plane-Point Postulate

A plane contains at least three noncollinear points.

2.6 Plane-Line Postulate

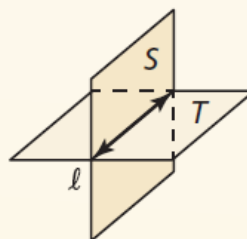
If two points lie in a plane, then the line containing them lies in the plane.



Points D and E lie in plane R , so \overleftrightarrow{DE} lies in plane R .

2.7 Plane Intersection Postulate

If two planes intersect, then their intersection is a line.



The intersection of plane S and plane T is line ℓ .

Point, Line, and Plane Postulates**Postulate****Example****2.1 Two Point Postulate**

Through any two points, there exists exactly one line.



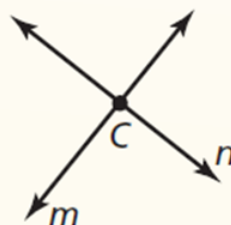
Through points A and B , there is exactly one line ℓ . Line ℓ contains at least two points.

2.2 Line-Point Postulate

A line contains at least two points.

2.3 Line Intersection Postulate

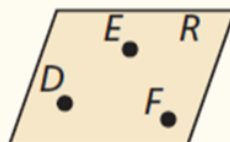
If two lines intersect, then their intersection is exactly one point.



The intersection of line m and line n is point C .

2.4 Three Point Postulate

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Through points D , E , and F , there is exactly one plane, plane R . Plane R contains at least three noncollinear points.

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A plane contains at least three noncollinear points.

2.6 Plane-Line Postulate

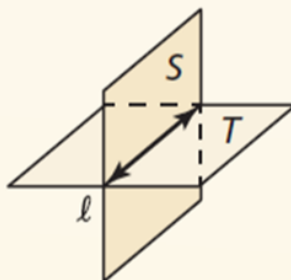
If two points lie in a plane, then the line containing them lies in the plane.



Points D and E lie in plane R , so \overleftrightarrow{DE} lies in plane R .

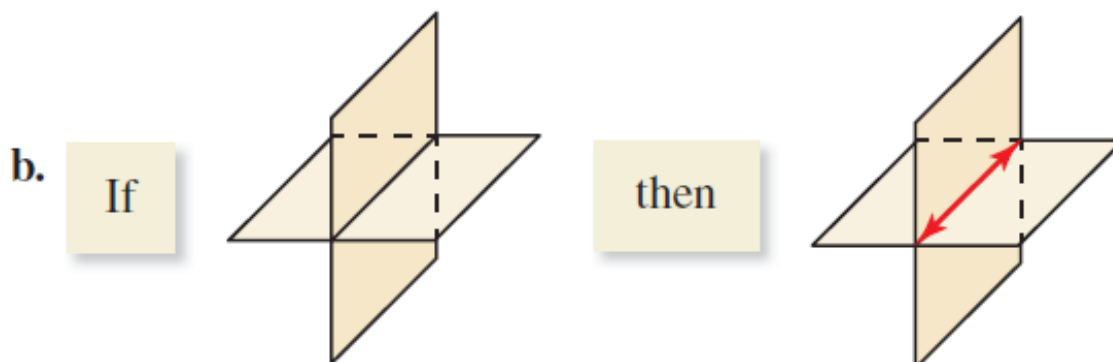
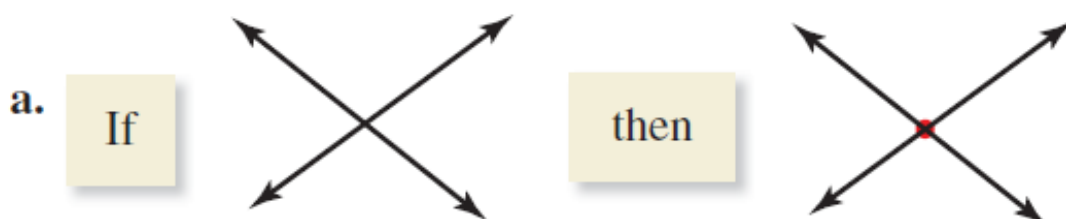
2.7 Plane Intersection Postulate

If two planes intersect, then their intersection is a line.

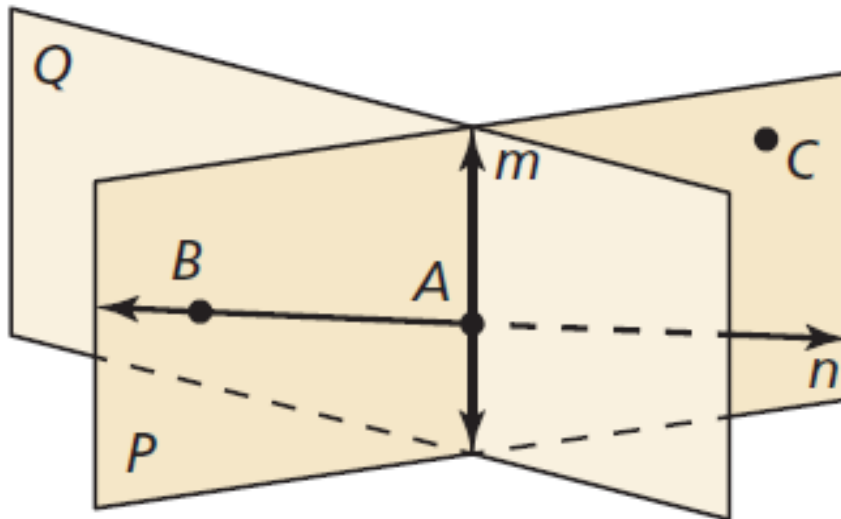


The intersection of plane S and plane T is line ℓ .

State the postulate illustrated by the diagram.



Use the diagram to write examples of the Plane-Point Postulate and the Plane-Line Postulate.



Sketch a diagram showing \overleftrightarrow{TV} intersecting \overline{PQ} at point W , so that $\overline{TW} \cong \overline{WV}$.

Which of the following statements *cannot* be assumed from the diagram?

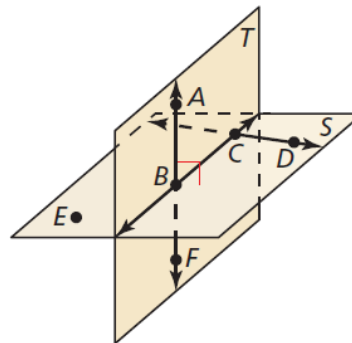
Points A , B , and F are collinear.

Points E , B , and D are collinear.

$\overline{AB} \perp$ plane S

$\overline{CD} \perp$ plane T

\overline{AF} intersects \overline{BC} at point B .



 **Core Concept****Algebraic Properties of Equality**

Let a , b , and c be real numbers.

Addition Property of Equality

If $a = b$, then $a + c = b + c$.

Subtraction Property of Equality

If $a = b$, then $a - c = b - c$.

Multiplication Property of Equality

If $a = b$, then $a \cdot c = b \cdot c$, $c \neq 0$.

Division Property of Equality

If $a = b$, then $\frac{a}{c} = \frac{b}{c}$, $c \neq 0$.

Substitution Property of Equality

If $a = b$, then a can be substituted for b
(or b for a) in any equation or expression.

 **Core Concept**
Reflexive, Symmetric, and Transitive Properties of Equality

	Real Numbers	Segment Lengths	Angle Measure
Reflexive Property	$a = a$	$AB = AB$	$m\angle A = m\angle A$
Symmetric Property	If $a = b$, then $b = a$.	If $AB = CD$, then $CD = AB$.	If $m\angle A = m\angle B$, then $m\angle B = m\angle A$.
Transitive Property	If $a = b$ and $b = c$, then $a = c$.	If $AB = CD$ and $CD = EF$, then $AB = EF$.	If $m\angle A = m\angle B$ and $m\angle B = m\angle C$, then $m\angle A = m\angle C$.

