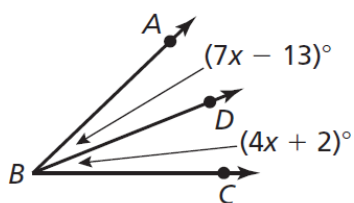
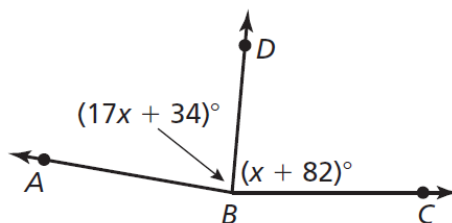


$\overline{BD}$  bisects  $\angle ABC$ . Find  $m\angle ABD$  and  $m\angle CBD$ .

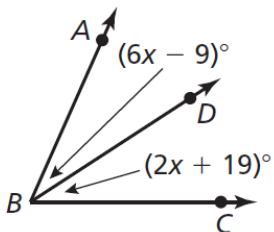
1.



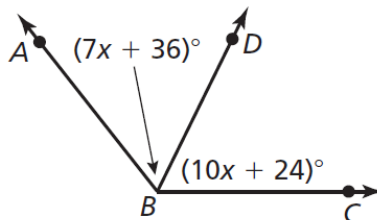
2.



3.



4.



## **Essential Question**

In a diagram, what can be assumed and what needs to be labeled?

$\overleftrightarrow{AF}$  and  $\overleftrightarrow{BD}$  are perpendicular.

$\overleftrightarrow{EG}$  and  $\overleftrightarrow{BD}$  are parallel.

$\overleftrightarrow{AF}$  and  $\overleftrightarrow{BD}$  are coplanar.

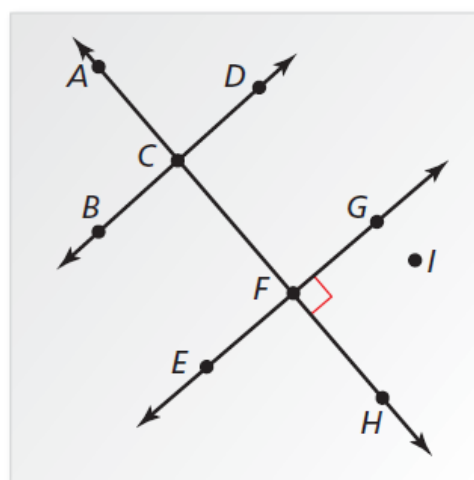
$\overleftrightarrow{EG}$  and  $\overleftrightarrow{BD}$  do not intersect.

$\overleftrightarrow{AF}$  and  $\overleftrightarrow{BD}$  intersect.

$\overleftrightarrow{EG}$  and  $\overleftrightarrow{BD}$  are perpendicular.

$\angle ACD$  and  $\angle BCF$  are vertical angles.

$\overleftrightarrow{AC}$  and  $\overleftrightarrow{FH}$  are the same line.



# Postulates

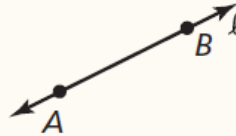
## Point, Line, and Plane Postulates

### Postulate

### Example

#### 2.1 Two Point Postulate

Through any two points, there exists exactly one line.



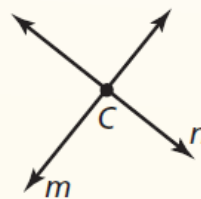
Through points  $A$  and  $B$ , there is exactly one line  $l$ . Line  $l$  contains at least two points.

#### 2.2 Line-Point Postulate

A line contains at least two points.

#### 2.3 Line Intersection Postulate

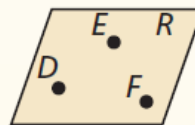
If two lines intersect, then their intersection is exactly one point.



The intersection of line  $m$  and line  $n$  is point  $C$ .

#### 2.4 Three Point Postulate

Through any three noncollinear points, there exists exactly one plane.



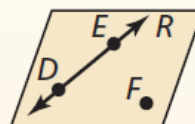
Through points  $D$ ,  $E$ , and  $F$ , there is exactly one plane, plane  $R$ . Plane  $R$  contains at least three noncollinear points.

#### 2.5 Plane-Point Postulate

A plane contains at least three noncollinear points.

#### 2.6 Plane-Line Postulate

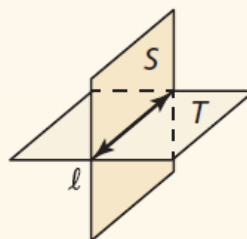
If two points lie in a plane, then the line containing them lies in the plane.



Points  $D$  and  $E$  lie in plane  $R$ , so  $\overline{DE}$  lies in plane  $R$ .

#### 2.7 Plane Intersection Postulate

If two planes intersect, then their intersection is a line.



The intersection of plane  $S$  and plane  $T$  is line  $l$ .

## Point, Line, and Plane Postulates

### Postulate

### Example

#### 2.1 Two Point Postulate

Through any two points, there exists exactly one line.



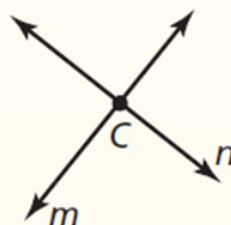
Through points  $A$  and  $B$ , there is exactly one line  $\ell$ . Line  $\ell$  contains at least two points.

#### 2.2 Line-Point Postulate

A line contains at least two points.

#### 2.3 Line Intersection Postulate

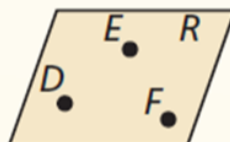
If two lines intersect, then their intersection is exactly one point.



The intersection of line  $m$  and line  $n$  is point  $C$ .

**2.4 Three Point Postulate**

Through any three noncollinear points, there exists exactly one plane.



Through points  $D$ ,  $E$ , and  $F$ , there is exactly one plane, plane  $R$ . Plane  $R$  contains at least three noncollinear points.

**2.5 Plane-Point Postulate**

A plane contains at least three noncollinear points.

**2.6 Plane-Line Postulate**

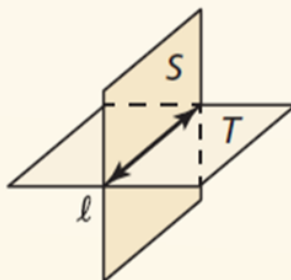
If two points lie in a plane, then the line containing them lies in the plane.



Points  $D$  and  $E$  lie in plane  $R$ , so  $\overleftrightarrow{DE}$  lies in plane  $R$ .

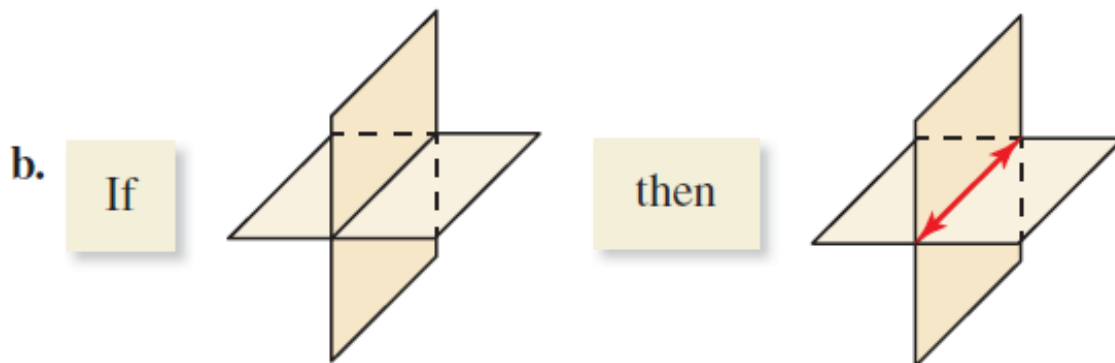
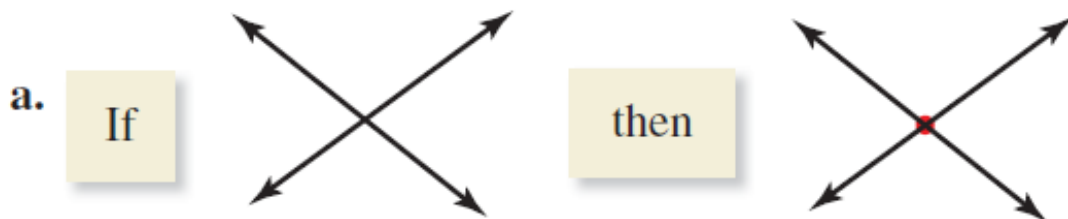
**2.7 Plane Intersection Postulate**

If two planes intersect, then their intersection is a line.

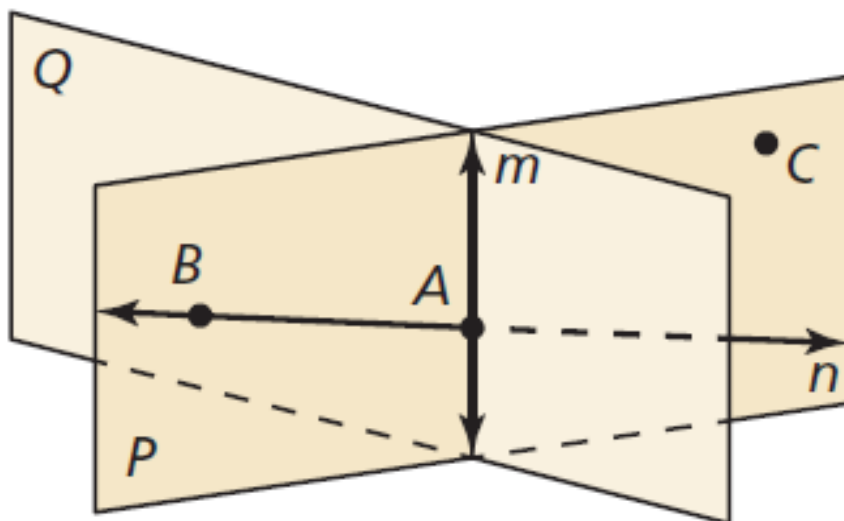


The intersection of plane  $S$  and plane  $T$  is line  $\ell$ .

State the postulate illustrated by the diagram.



Use the diagram to write examples of the Plane-Point Postulate and the Plane-Line Postulate.





Sketch a diagram showing  $\overleftrightarrow{TV}$  intersecting  $\overline{PQ}$  at point  $W$ , so that  $\overline{TW} \cong \overline{WV}$ .

Which of the following statements *cannot* be assumed from the diagram?

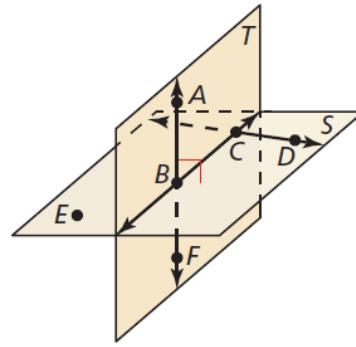
Points  $A$ ,  $B$ , and  $F$  are collinear.

Points  $E$ ,  $B$ , and  $D$  are collinear.

$\overline{AB} \perp$  plane  $S$

$\overline{CD} \perp$  plane  $T$

$\overline{AF}$  intersects  $\overline{BC}$  at point  $B$ .



 **Core Concept****Algebraic Properties of Equality**

Let  $a$ ,  $b$ , and  $c$  be real numbers.

**Addition Property of Equality**

If  $a = b$ , then  $a + c = b + c$ .

**Subtraction Property of Equality**

If  $a = b$ , then  $a - c = b - c$ .

**Multiplication Property of Equality**

If  $a = b$ , then  $a \cdot c = b \cdot c$ ,  $c \neq 0$ .

**Division Property of Equality**

If  $a = b$ , then  $\frac{a}{c} = \frac{b}{c}$ ,  $c \neq 0$ .

**Substitution Property of Equality**

If  $a = b$ , then  $a$  can be substituted for  $b$  (or  $b$  for  $a$ ) in any equation or expression.


**Core Concept**
**Reflexive, Symmetric, and Transitive Properties of Equality**

	Real Numbers	Segment Lengths	Angle Measure
<b>Reflexive Property</b>	$a = a$	$AB = AB$	$m\angle A = m\angle A$
<b>Symmetric Property</b>	If $a = b$ , then $b = a$ .	If $AB = CD$ , then $CD = AB$ .	If $m\angle A = m\angle B$ , then $m\angle B = m\angle A$ .
<b>Transitive Property</b>	If $a = b$ and $b = c$ , then $a = c$ .	If $AB = CD$ and $CD = EF$ , then $AB = EF$ .	If $m\angle A = m\angle B$ and $m\angle B = m\angle C$ , then $m\angle A = m\angle C$ .

